

Study the Effect of SRRs on Broadband Microwave Parallel-Coupled Band-Pass Filters

Ahmed Hameed Reja, Syed Naseem Ahmad, and Mushtaq A. Alqaisy

Abstract—In this paper, broadband microwave parallel-coupled band-pass filters for wireless microwave technology are presented. Two designs of filters with center frequency of 10.5GHz and 9.5GHz are proposed. A metallic split ring resonator (SRR) as a basic building block for planar filters with dual-band band-pass frequency response, which exhibits simultaneously negative permittivity and permeability as a metamaterial without resorting to additional metallic wires is numerically investigated. The effect of SRRs on these filters to get new two metamaterial dual-band microwave filters is also presented. The dimensions of the second filter are reduced compared to the first filter with better results. Numerical results for all designs are obtained, then the filters are simulated using computer aided design (CAD) in microwave applications (Ansoft HFSS) and implemented on the Roger RT/duroid 6010, dielectric constant $\epsilon_r=10.2$, and a substrate height $t = 0.635\text{mm}$.

Index Terms—Metamaterial, microwave filter, parallel-coupled, split ring resonators.

I. INTRODUCTION

The band-pass filter (BPF) has many applications in a microwave system. It serves well in reducing the noise and harmonic content of a system by limiting the band of frequencies seen by the system. Many times, band-pass filters are placed at the front end of a receiver to decrease the out of band noise that can enter. They can be used at the output of a transmitter to reduce or eliminate harmonics and spurious outputs generated within the system [1]. A band-pass filter passes a specific band of frequencies and rejects frequencies below and above that band. The response curve of a band-pass filter is shown in Fig. 1. This response shows an area that is termed the pass-band, which is the area where there is a minimum loss in the filter response [2]. The ratio of the power delivered from a source to a load with and without a two-port network inserted in between is known as the insertion loss of that two-port. The fraction of the input power that is lost due to reflection at its input port is called the return loss. The ratio of the power delivered to a matched load to that supplied to it by a matched source is called the attenuation of that two-port network [3].

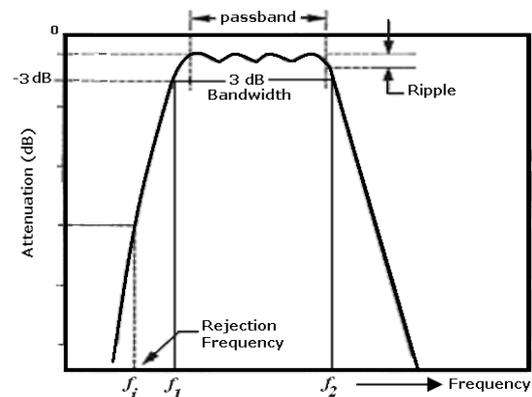


Fig. 1. Band-pass filter response

Metamaterials (MTMs) are defined as artificial (fabricated by human), effectively homogeneous ($p \ll \lambda_g$) and exhibiting highly unusual properties ($\epsilon_r, \mu_r < 0$) not readily available in nature, where p is the average cell size and it is much smaller than the guided wavelength (λ_g) [4].

Split-ring resonators (SRR) were one of the first particles proposed for metamaterial construction. Metallic metamaterials comprising double split-ring resonators (SRRs) are the main artificial structures to realize magnetic responses at an electromagnetic spectrum above gigahertz frequencies [5]-[8]. The realization of backward wave propagation using split ring resonator (SRR) and thin wire (TW) and several other electrically small resonators was considered by Pendry *et al.* [5], [9]. The split ring resonator shown in Fig. 2 is used to obtain a negative value of effective permeability over a desired frequency range.

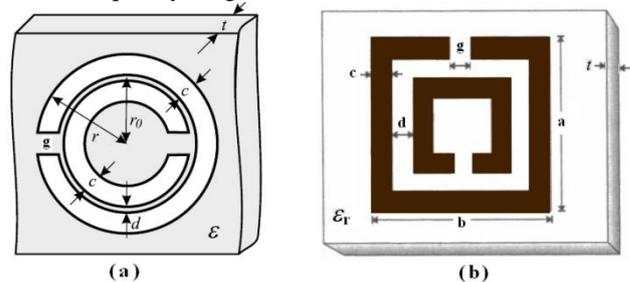


Fig. 2. SRR topology (a) Circle shape, (b) Square shape. The relevant dimensions are indicated.

A kind of LHM, consisting of split ring resonators (SRRs) and continuous wires, whose properties were not determined by the fundamental physical properties of their constituents but the shape and distribution of specific patterns included, was fabricated by Shelby *et al.* [10] based on Pendry's research. The idea for the implementation of the first MTM TL based on SRRs has been presented by Martin *et al.* [11]. The SRRs has negative permeability at specific resonance frequency, which can be proved mathematically. This negative permeability can prevent wave propagation at the

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resonant frequency because wave direction is reverse.

In addition to the capability of SRR to generate a negative permeability ($\mu_{eff} < 0$), the SRR should be of capability to produce a negative permittivity ($\epsilon_{eff} < 0$) at certain frequencies instead of cut wires. Consequently, a metamaterial composed of SRRs could be an LHM when the negative permeability and permittivity are modulated to a common frequency band. However, this is typically difficult to design [12], [13].

In fact the presence of SRRs in the active region of the filters affects somewhat the electrical characteristics of the structures. It has been found that the presence of SRRs in the parallel coupled-line filters modifies the characteristics of the coupled-line sections as compared to the structures without SRRs. Therefore, it is necessary to recalculate dimensions to preserve the central filter frequency and bandwidth [14].

Parallel-coupled microstrip filters have been widely used for decades in the RF front end of wireless communication systems. The design method for parallel-coupled microstrip filters is presented in [15], [16]. There are many published papers on parallel-coupled band-pass filters using different techniques and different frequencies [17]-[20].

In this paper, four broadband parallel-coupled microwave filters are proposed. The first design operates at 10.5GHz center frequency and has pass-band of (8-13) GHz with minimum attenuation of -37.5dB at 1.4GHz. The specifications of Broadband filter are given in the Table I.

The designed filter is used in microwave wireless applications such as satellite television receivers. The design of filters using Ansoft HFSS software design and implemented on Roger RT/duroid, PTFE substrate with dielectric constant $\epsilon_r=10.2$, loss tangent $\tan\alpha = 0.0023$ and substrate height $t = 0.635\text{mm}$.

TABLE I: BROADBAND PASS FILTER DESIGN SPECIFICATION

Filter specifications	Values
Center frequency, f_o	10.5 GHz
Upper cut-off frequency, f_2	13 GHz
Lower cut-off frequency, f_1	8 GHz
Bandwidth	5 GHz
Minimum attenuation	-37.5dB at 1.4GHz

To obtain a new band-pass filter, the above designed filter is modified using U-shape resonator which miniaturizes the dimensions and gives better results at 9.5 GHz center frequency. The effects of SRRs on filters to get dual-band filter around center frequency are also presented. In addition, a left-handed response with simultaneously negative permittivity (ϵ_{eff}) and permeability (μ_{eff}) for getting negative refractive index using metallic SRRs is investigated.

II. PARALLEL-COUPLED FILTER DESIGN

The first step in designing a filter is to determine the fractional bandwidth (δ) as follows [21].

$$\delta = \frac{f_2 - f_1}{f_o} \quad (1)$$

f_1 , f_2 and f_o are the lower-, upper- cutoff frequency and center frequency respectively.

The frequency transformation from the low-pass prototype filter to the band-pass filter is expressed as

$$\frac{f}{f_c} = \frac{2}{\delta} \left(\frac{f_i - f_o}{f_o} \right) \quad (2)$$

where f_c is the prototype cutoff frequency (equal to 1.0) and filter frequency (f) has to be defined in the filter specification. A fractional bandwidth of 0.4762 and transformation ratio of -3.64 should be obtained. The second step is examining the filter prototype specification which meets the insertion loss requirements. The family of curves shown in Fig. 3 applies to Chebyshev prototypes all giving a -0.01dB pass-band ripple.

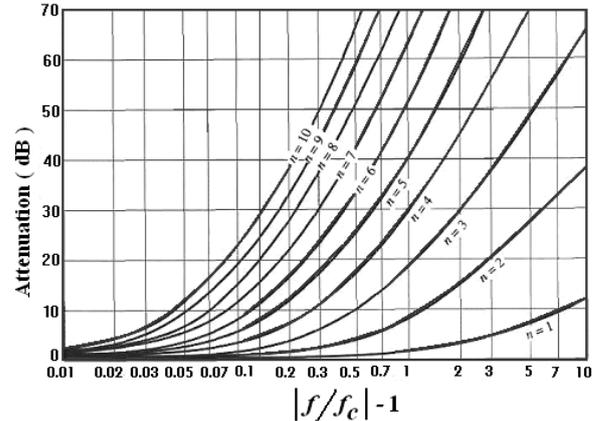


Fig. 3. Attenuation versus normalized frequency.

The independent variable has been adjusted as

$$\left| \frac{f}{f_c} \right| - 1 \quad (3)$$

From the Fig. 3, the value of $|f/f_c| - 1$ is found to be 2.64. A third order ($n = 3$) design therefore gives a -37.5 dB insertion loss of f_i , this is equivalent to the 1.4GHz point in the final requirement. For ripple amplitude $R > 0.01\text{dB}$, only odd order designs are permissible, ensuring that $g_o = g_n = 1$ accurate. The equations for the calculation of element values (g_n) are given below [19].

$$g_1 = \frac{2}{\gamma} \sin\left(\frac{\pi}{2n}\right) \quad (4)$$

$$g_i = \frac{1}{g_{i-1}} \frac{4 \sin\left[\frac{(2i-1)\pi}{2n}\right] \sin\left[\frac{(2i-3)\pi}{2n}\right]}{\gamma^2 + \sin^2\left[\frac{(i-1)\pi}{n}\right]} \quad (5)$$

for $i = 2, 3, \dots, n$

$$g_{n+1} = \begin{cases} 1.0 & \text{for } n \text{ odd} \\ \coth^2\left(\frac{\beta}{4}\right) & \text{for } n \text{ even} \end{cases} \quad (6)$$

where

$$b = \ln\left[\coth\left(\frac{R}{17.37}\right)\right]$$

$$g = \sinh\left[\frac{b}{2n}\right]$$

Based on the design specification, a 10.5GHz center frequency filter is required for microwave wireless receiver

such as satellite television receivers. The element values obtained are given in the Table II.

TABLE II: ELEMENTS VALUES OF PARALLEL-COUPLED FILTER

g_0	g_1	g_2	g_3	g_4
1	1.0316	1.1474	1.0316	1

The third step is to calculate the inverter admittances (normalized for 50Ω impedance) and hence coupled-line impedances use the following equations [15, 21].

$$Z_o J_1 = \sqrt{\frac{\pi\delta}{2g_o g_1}} \quad (7)$$

$$Z_o J_n = \frac{\pi\delta}{2\sqrt{g_{n-1} g_n}} \quad (8)$$

for $n = 2, 3$

$$Z_o J_{n+1} = \sqrt{\frac{\pi\delta}{2g_n g_{n+1}}} \quad (9)$$

$$Z_{oe} = Z_o \left[1 + JZ_o + (JZ_o)^2 \right] \quad (10)$$

$$Z_{oo} = Z_o \left[1 - JZ_o + (JZ_o)^2 \right] \quad (11)$$

where

$$Z_o \approx \sqrt{Z_{oe} Z_{oo}} \quad (12)$$

J is the inverter, Z_o is the system characteristic impedance, Z_{oe} is the even characteristic impedance and Z_{oo} is the odd characteristic impedance. All results are indicated in the Table III.

TABLE III: PARAMETERS OF PARALLEL-COUPLED FILTER

n	$Z_o J_n$	$Z_{oe}(\Omega)$	$Z_{oo}(\Omega)$	$Z_o(\Omega)$
1	0.8515	128.83	43.68	75.01
2	0.6875	108	39.25	65.11
3	0.6875	108	39.25	65.11
4	0.8515	128.83	43.68	75.01

III. NUMERICAL AND SIMULATION RESULTS

A. Parallel-Coupled Microwave Filters

Table I indicates the specifications of the broadband microwave parallel-coupled filter design. Using (4) - (6) to find the elements value g_n which indicates in the table II. Then calculate the value of even and odd characteristic impedances (Z_{oe} , Z_{oo}) from (10) & (11). After finding the values of Z_o in (12) for each element and by using standard chart [21] or tables in [22] with some approximation, we get the values of w/h and s/h for each element. The dimensions of layout design of parallel-coupled microwave band-pass filter are indicated in the Table IV.

TABLE IV: SIMULATION DIMENSIONS OF COUPLED-LINES FOR THE DESIGN IN FIGURE 4 WHICH INDICATES THE ELEMENTS NUMBER

Element Number	W (mm)	L (mm)	S (mm)
1=8	0.75	2	$S_1 = S_2 = 0.04$
2=3=6=7	0.169	3.38	
4=5	0.5564	2	$S_3 = 0.076$

The layout design shown in Fig. 4 has the dimensions $12.76\text{mm} \times 3\text{mm} \times 0.705\text{mm}$.

The insertion and return loss at -3dB for the band (8-13)

GHz and the rejection frequencies are shown in Fig. 5. The modified design has the same dimensions of elements and spacing as compared with the first design but eliminate layout dimensions as a modified shape, which is shown in Fig. 6.

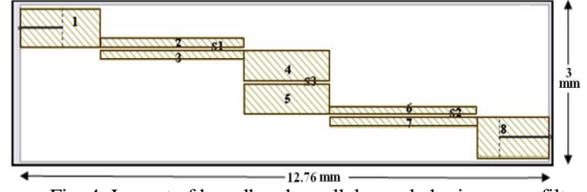


Fig. 4. Layout of broadband parallel-coupled microwave filter.

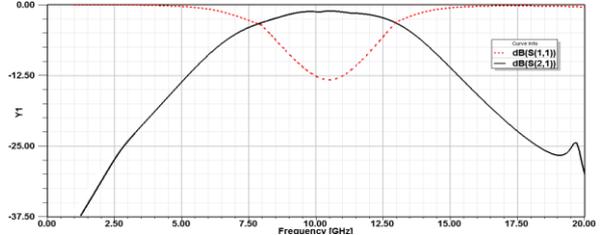


Fig. 5. Filter response simulation for broadband parallel-coupled microwave filter.

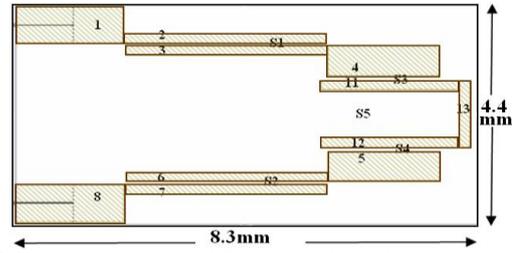


Fig. 6. Modified design of wideband parallel-coupled microwave filter.

The separation of the U-shape resonator is chosen with the aid of software (Ansoft HFSS) and listed in Table V. If the separation is chosen to be too small, there will be a lot parasitic reactance. If the separation is too big, losses will be great. Therefore a balance between the two has to be met [19]. The U-shape resonator makes a shift in center frequency to become 9.5GHz that means miniaturize in dimensions. The overall dimensions of the modified filter are $(8.3\text{mm} \times 4.4\text{mm} \times 0.705\text{mm})$.

TABLE V: SIMULATION DIMENSIONS OF MODIFIED FILTER DESIGN

Element Number	W (mm)	L (mm)	S (mm)
1=8	0.75	2	$S_1 = S_2 = 0.05366$ $S_3 = S_4 = 0.108$ $S_5 = 0.9927$
2=3=6=7	0.187	3.6	
4=5	0.59	2	
11=12	0.187	2.68	
13	0.202	0.992	

The insertion loss (S_{21} -dB) and return loss (S_{11} -dB) of modified filter are shown in Fig. 7. A band-pass of 7.5GHz bandwidth at 9.5GHz center frequency and stop-band 6.5GHz bandwidth at 16GHz center frequency.

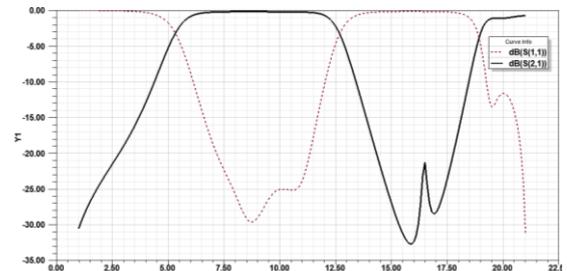


Fig. 7. Filter response simulation for modified parallel-coupled filter.

B. SRR Structure

The metallic SRRs metamaterial are shown in Fig. 8. The split rings are copper in a square with a thickness of 0.035mm and the geometric parameters (a)=(b) are 1.5mm. In Fig. 8-a, the parameter (c) is 0.11mm, the gap between the inner and outer rings, represented by (d), is 0.12mm, and each of the splits in the inner and outer rings has the same width (g) of 0.15 mm. In Fig. 8-b, the parameters (c), (d) and (g) are 0.15mm, 0.05mm and 0.15 mm respectively.

The SRR is electrically very compact due to use of sub-wavelength structure (generally $\leq \lambda/10$) but in our design the sub-wavelength approximate to $\lambda/20$.

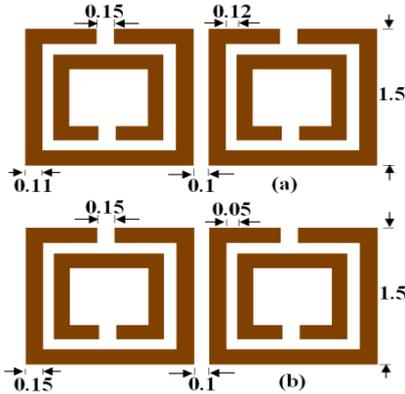


Fig. 8. Metallic SRRs metamaterial (a) at 10.5GHz, (b) at 9.5GHz. All values are indicated in (mm).

The transmission coefficient (S_{21} -dB) of the double ring metamaterial is shown in Fig. 9. It is obvious that there are a stop-band around 10.5 GHz and 9.5 GHz that is shown in Fig. 9 (a), and 9(b) respectively.

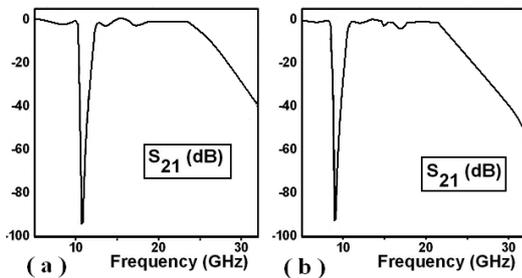


Fig. 9. Transmission coefficient of the metallic SRRs metamaterial. The stop-band at (a) 10.5GHz, (b) 9.5GHz.

The calculation was performed to obtain the ϵ_{eff} and μ_{eff} from the scattering parameters (S_{21} and S_{11}) of the proposed SRR metamaterial [23], [24]. Fig. 10 shows the ϵ_{eff} and μ_{eff} respect to frequency for the metallic SRRs. It is also obvious that the retrieved negative μ_{eff} and positive ϵ_{eff} in the fundamental resonant regime are contributing to the stop-band near 10.5GHz and 9.5GHz that is shown in Fig. 10(a), and 10(b) respectively.

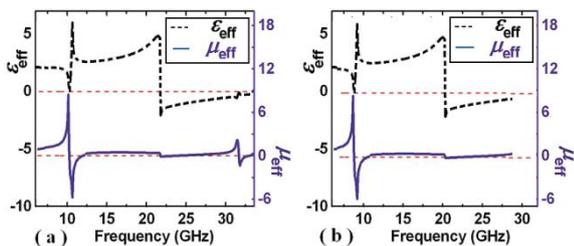


Fig. 10. Effective permittivity and permeability of the metallic SRRs metamaterial (a) stop-band near 10.5GHz, (b) stop-band near 9.5GHz.

C. Metamaterial Parallel-Coupled Microwave Filters

After adding metallic SRRs structures to our designs as shown in Fig. 11, and Fig. 13 we saw the obvious changes in responses. So, we got on stop-band at around the center frequency to cut the previous BPF to dual-band operate at 7.5GHz with 3GHz bandwidth and 12.5GHz with 2GHz bandwidth that is shown in Fig. 12.

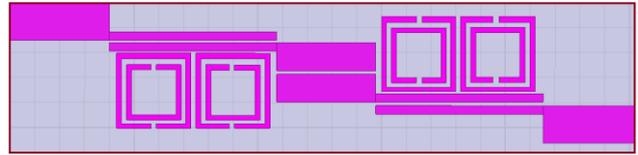


Fig. 11. Layout of metamaterial dual-band band-pass filter.

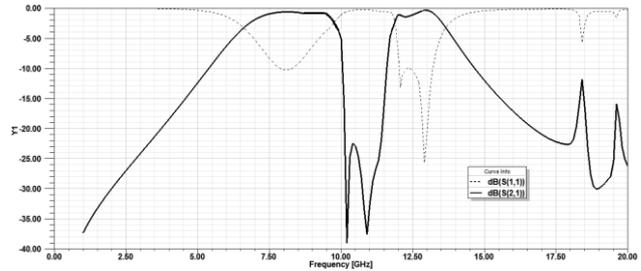


Fig. 12. The response of metamaterial dual-band band-pass filter.

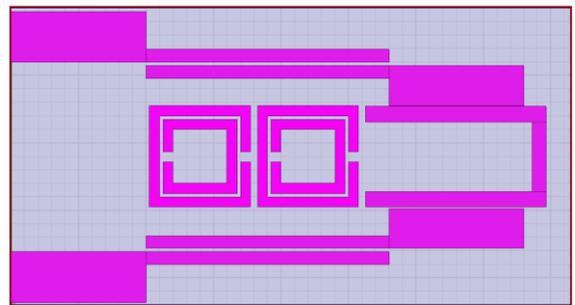


Fig. 13. Layout of modified metamaterial dual-band band-pass filter.

From Fig. 14 we got on stop-band around the certain frequency to cut the previous band-pass filter to dual-band operate at 8.2GHz with 2.5GHz bandwidth and 11GHz with 3.5 GHz bandwidth.

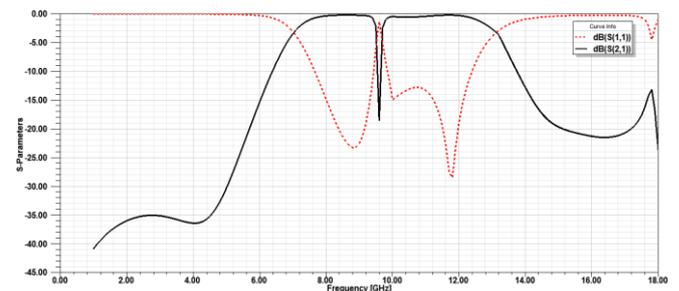


Fig. 14. The response of the modified metamaterial filter contains U- shape structure.

IV. CONCLUSIONS

In this paper, two designs of broadband parallel- coupled microwave band-pass filters have been presented. The effect of SRRs on filters is also presented. All designs are carried out by analysis and simulation using Ansoft HFSS software. The numerical results agreed well with the simulation results. Numerical results show that a rejection level of almost -37.5dB at pass-band frequency can be obtained when using a substrate material of RT/duroid 6010, $\epsilon_r=10.2$, $\tan\alpha=0.0023$,

$t = 0.635\text{mm}$ with input impedance equal to 50Ω . Also the results in the second design (modified) are better compared to the first design. The U-shape resonator in the modified design gives wider bandwidth and also the center frequency is shifted from 10.5GHz to 9.5GHz. The response of metallic SRRs metamaterial is numerically investigated. The presence of SRRs in the parallel coupled-line filters modifies the characteristics of the coupled-line sections as compared to the structures without SRRs. Therefore, it is necessary to recalculate dimensions to preserve the central filter frequency and bandwidths. Finally apply this structure (SRR) in filter design to get dual-band-pass or stop-band around the center frequency with high return loss.

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